Multipoint Channel Charting for Wireless Networks

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Abstract—Multipoint channel charting is a machine learning framework in which multiple massive MIMO (mMIMO) base-stations (BSs) collaboratively learn a multi-cell radio map that characterizes the network environment and the users’ spatial locations. The method utilizes large amounts of high-dimensional channel state information (CSI) that is passively collected from spatiotemporal samples by multiple distributed BSs. At each BS, a high-resolution multi-path channel parameter estimation algorithm extracts features hidden in the acquired CSI. Each BS then constructs a local dissimilarity matrix based on the extracted features for its collected samples and feeds it to a centralized entity which performs feature fusion and manifold learning to construct a multi-cell channel chart. The objective is to chart the radio geometry of a cellular system in such a way that the spatial distance between two users closely approximates their CSI feature distance. We demonstrate that (i) multipoint channel charting is capable of unravelling the topology of a Manhattan-grid system and (ii) the neighbor relations between CSI features from different spatial locations are captured almost perfectly.

I. INTRODUCTION

Massive multiple-input multiple-output (mMIMO) provides cellular systems with high spectral efficiency [1]. The idea of mMIMO is to equip the infrastructure base-stations (BSs) with hundreds of antennas, which simultaneously serve tens of user equipments (UEs) in the same frequency band. In addition to increasing spectral efficiency, the high spatial resolution provided by the large-scale antenna array used at the mMIMO BSs can be exploited for a range of sensing applications, such as UE positioning and tracking [2]–[4], UE orientation estimation [5], and environment mapping [6], [7].

A. Channel Charting

Channel state information (CSI) acquired at the mMIMO BSs, especially the slowly changing channel mean and covariance matrices, depend continuously on the spatiotemporal locations of UEs, as well as the effective radio reflectors and scatters in the physical channel. As a result, the aggregate spatiotemporal CSI contains useful information about the network states including the spatial distribution and trajectories of the UEs, neighborhood relationships among the UEs, and handover relationships among neighboring cells. The massive amount of mMIMO CSI, if collected and stored at the BSs, can potentially be leveraged to learn such network state information, which in turn can be exploited to automate cellular radio resource management (RRM) functions.

To leverage mMIMO CSI for RRM functions, reference [2] proposed the concept of channel charting, which analyzes CSI acquired at a single BS with tools from dimensionality reduction and manifold learning in order to construct a channel chart of the wireless channel that relates physical UE location to CSI. The core idea behind channel charting is that UEs which are close in geographic space would experience similar CSI (e.g., channel mean and covariance) at a BS.

B. Contributions

Channel charting could be performed by each BS independently with the original method discussed in [2]. Different BSs would produce differing channel charts for the same UE samples due to different channel realizations and signal-to-noise ratios (SNRs). However, to support advanced multi-cell RRM functions, such as handover and multi-connectivity, a single-point chart is insufficient. Furthermore, single-point channel charting may be inaccurate for CSI from cell-edge UEs as their low SNRs may distort the charting results. As a remedy to these limitations, we propose multipoint channel charting in which multiple mMIMO BSs collaboratively learn a channel chart for UEs in the multi-cell network. Based on CSI acquired at multiple BSs, multipoint channel charting builds a common multi-cell channel chart which merges the views of all BSs by applying the concepts of multi-view ML and data fusion. As we will show, multipoint channel charting is able to produce trustworthy channel charts by combining all CSI available at multiple BSs and by exploiting redundancy in multipoint CSI in order to combat the distortion which occurs in single-point channel charting results.

II. MULTIPONT CHANNEL CHARTING FRAMEWORK

UEs move in two related geometries: (i) the conventional spatial geometry, i.e., the spatial position in the real world, and (ii) the radio geometry is related to the radio environment between the transmitter and receiver, i.e., represented by CSI of the radio link between the UE and BS. Changes of CSI reflects the location of the UE, and its temporal change in the spatial geometry. Consider a single-antenna UE $k$, transmitting a specific pilot signal $s_{k,t}$ with time stamp $t$. A mMIMO BS equipped with $M$ antenna elements receives the pilot the signal for channel estimation. For simplicity, we consider a uniform linear array (ULA) at the BS. Then, for a single coherence bandwidth, the channel vector can be modeled [8] as

$$h = \sum_{l=1}^{L} \beta_l a_{\text{BS}}(\phi_l),$$ (1)

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where $L$ is the number of multi-path components (including the LoS ray if it exists) which are created by the radio scatters, $\varphi_l$ is the impinging direction-of-arrival (DoA) of the $l$th propagation path related to the orientation of the BS array, and $\beta_l$ a random complex gain for the $l$th path which depends on the transmit power, path delays, reflection coefficients of the contributing scatters, and impacts of radio chain components. In addition, the vector $a_{BS}(\phi)$ represents the BS array steering vector (ASV) which depends on the geometry of the entire array and the incident angle $\phi$. For a ULA with the plane-wave approximation, the ASV is given by

$$a_{BS}(\phi) = [1, e^{j\frac{2\pi}{\lambda} s \sin(\phi)}, \ldots, e^{j(M-1)\frac{2\pi}{\lambda} s \sin(\phi)}]^T,$$

where $M$ is the number of BS antennas, $\lambda$ is the carrier wavelength, and $s$ is the antenna spacing.

Noticing that the DoAs $\{\varphi_l\}_{l=1}^L$ and the powers $\{\beta_l^2\}_{l=1}^L$ change much more slowly and smoothly with the UE movements as compared to the coefficients of $h$, it is worth considering the raw 2nd moment (covariance) of $h$ [2], which depends on $\{\phi_l\}_{l=1}^L$ and $\{\beta_l^2\}_{l=1}^L$ as

$$Y = \mathbb{E}[hh^H] = \mathbb{E} \sum_{l=1}^{L} |\beta_l|^2 a_{BS}(\phi_l)a_{BS}^H(\phi_l)$$

$$= \text{ASAV}^H \in \mathbb{C}^{M \times M},$$

with $A = [a_{BS}(\phi_1) \cdots a_{BS}(\phi_L)]$ a matrix of the array steering vectors, and $S = \text{diag}(\mathbb{E}[|\beta_1|^2], \ldots, \mathbb{E}[|\beta_L|^2])$ containing the powers of all multi-path components. The covariance matrix can be estimated from time/frequency samples as $\hat{Y} = T^{-1} \sum_{t=1}^{T} h_t h_t^H$, where $T$ is the number of time stamps one averages over. In wideband channels, the covariance can be calculated across multiple coherence bandwidths.

The spatiotemporal samples $\{Y_n\}_{n=1}^N$ are the CSI collected at the $b$th BS ($b = 1, \ldots, B$) from $N$ UE locations $\{p_n\}_{n=1}^N$. In a static radio environment with omnidirectional antennas and fixed transmit power, the covariance depends solely on the UE spatial location. As detailed in [2], a key assumption enabling channel charting is that there is a (statistical) mapping from spatial location $p_n$ to covariance CSI $Y_n^b$ measured at the $b$th mMIMO BS:

$$\mathcal{H}^b : \mathbb{R}^d \rightarrow \mathbb{C}^D; \quad \mathcal{H}^b(p_n) = Y_n^b,$$

where $D = M \times M$ is the dimensionality of the radio geometry over $\mathbb{C}$. Thus, the CSI $Y_n^b$ depends on the specific spatial location $p_n$. In addition, we assume that this mapping is continuous, i.e., the CSI related to two nearby spatial locations is similar. This mapping depends on the distributions and dielectric properties of the static reflectors, scatterers, and blockages in the radio network environment. Given the CSI samples $\{Y_n^b\}_{n=1}^B$ collected at $B$ mMIMO BSs from $N$ unknown random spatial locations $\{p_n\}_{n=1}^N$, we are interested in finding a low-dimensional channel chart $\{z_n\}_{n=1}^N$ with $z_n \in \mathbb{R}^d$, such that

$$\|z_n - z_m\|_2 \approx \alpha \|p_n - p_m\|_2,$$

for $n, m \in \{1, 2, \ldots, N\}$, where $\alpha$ is a common scaling factor.

Figure 1 depicts the overall framework for multi-point channel charting. The $b$th mMIMO BS collects CSI samples from its coverage area and has its own local view on the distribution of the samples it observes. A feature extraction function that distills useful information $\{f_n^b\}_{n=1}^N$ from the raw UE CSI $\{Y_n^b\}_{n=1}^N$ is applied. These features $\{f_n^b\}_{n=1}^N$ are then used to compute a local dissimilarity matrix $D^b$. The dissimilarity matrix $D^b$ represents the local view on the CSI at BS $b$, related to radio distances between the sampled points. Note that different BSs will have different views on the samples. First, different BSs observe different parts of the entire CSI sample set in the network due to different cellular coverage areas. Second, different BSs may have different opinions on the dissimilarity for the same sample pair due to different channel conditions, e.g., different SNR conditions. One BS may have more reliable information on the CSI of a specific UE than another BSs if the channel conditions between this BS and
the UE are better. To construct a global and reliable multi-cell channel chart, we have to fuse the data produced by different BSs. In this regard, a global dissimilarity matrix $D$ is then constructed based on $\{D^{B}_{l}\}_{B=1}^{L}$ from the $B$ BSs by a logical centralized unit (CU) that takes into account a reliability factor. Finally, dissimilarity-matrix-based manifold learning is used to generate the multi-cell channel chart.

III. CSI FEATURES AND DISSIMILARITY

To learn a channel chart that reflects the spatial locations of the CSI samples, we need a feature that is smoothly changing with the UE location. The DoAs $\{\phi_{l}\}_{l=1}^{L}$ and powers $\{||\beta_{l}||^{2}\}_{l=1}^{L}$ of the multi-path components in (1) are such features.

In channel charting, we are interested in the dissimilarities among large-scale CSI samples rather than the physical position of a single UE. Differing from conventional positioning techniques, multi-path effects can be exploited in channel charting as locations close in spatial geometry would have similar multi-path components. By using an elaborate dissimilarity metric for these multi-path features, spatial relationships among the sample locations can be revealed by channel charting.

A. Feature Extraction via MUSIC

The multiple signal classification (MUSIC) algorithm [9] is widely used for DoA and frequency spectrum estimation. Here, we use MUSIC for channel feature extraction. The input of the algorithm is the covariance matrix of the data and it can be used for arbitrary antenna array geometries, as long as the relative antenna positions are known. Assuming that the number of antennas $M$ is larger than the number of multi-path components $L$, the array steering vectors for the $L$ paths are linearly independent, and that the signal $h$ and noise $e$ are orthogonal, the estimated covariance matrix is

$$\hat{Y} = E[ (h + e)(h + e)^H ] = Y + \sigma_e^2 I_M,$$

where $\sigma_e^2$ is the power of each entry of $e$. The signal covariance matrix $Y = ASA^H$ has a rank $L$; it therefore has $L$ eigenvectors with nonzero eigenvalues in the signal subspace, and $M - L$ eigenvectors corresponding to the zero eigenvalue. Let $Y = U\Lambda U^H$ be the eigendecomposition of $Y$, it can be proved that the estimated covariance matrix has the eigendecomposition $\hat{Y} = U(\Lambda + \sigma_e^2 I_M)U^H$ [9]. Using this eigendecomposition, we can partition the eigenvector matrix $U$ into two parts as $U = [U_n U_b]$, where $U_n$ of size $M \times L$ defines the signal subspace, while $U_b$ of size $M \times (M - L)$ defines the noise subspace.

The core idea of MUSIC is to find the signal directions using the so-called pseudo-spectrum

$$p(\phi) = \frac{1}{a_{BS}^{H}(\phi)U_n U_n^H a_{BS}(\phi)} = \frac{1}{||U_n^H a_{BS}(\phi)||_2^2}. \quad (7)$$

If $\phi$ equals one of the DoAs of the multi-path components, then the denominator is small. Therefore, the estimated DoAs are the $L$ largest peaks in the pseudo-spectrum. In practice, the number of paths $L$ is unknown, and it is estimated based on the eigen-decomposition of $\hat{Y}$. The path powers are estimated as the $L$ largest eigenvalues in the eigen-decomposition. To pair the estimated DoAs and the path powers, one can check the correlations between the eigenvectors for the powers and the array steering vectors for the DoAs. Finally, we get a channel feature vector $f = [\lambda_1, \lambda_2, \ldots, \lambda_L, \phi_1, \phi_2, \ldots, \phi_L] \in \mathbb{R}^{2L}$ for each BS-to-UE pair, where $\hat{L}$ is the estimated number of significant channel paths.

B. Dissimilarity Metric

Each BS extracts a feature set $\{f^{B}_n\}_{n=1}^{N}$ via MUSIC for the sampled UE locations. In what follows, we define a novel dissimilarity metric for the pairs of CSI samples based on the proposed feature. A good dissimilarity metric $d_{J}(f^{B}_{n}, f^{B}_{m})$ for two CSI samples $n$ and $m$ should be proportional to the real spatial distance $||p_n - p_m||_2$.

For two CSI features $f^{B}_{n} = [\mu_1, \ldots, \mu_{L_x}, \theta_1, \ldots, \theta_{L_y}]$, we need to identify the paths for the sample pair that are similar, being created by, for example, the same clusters. For this, we transform the path DoA and power pairs to points in a cartesian coordinate system according to

$$F(f^{B}_{n}) = [x_1, \ldots, x_{L_x}], \quad F(f^{B}_{m}) = [y_1, \ldots, y_{L_y}], \quad (8)$$

with $x_i = [\cos \phi_i, \sin \phi_i]^T$, $y_j = [\cos \theta_j, \sin \theta_j]^T$. If the channel rays were known, one could classify these cartesian points into LoS, single-bounce and double-bounce points according to the reflection orders for their corresponding multi-path components. To produce dissimilarity metrics in an unsupervised setting, it is worth noting that nearby UE locations would produce similar cartesian points as they share common scatters and have similar multi-path components.

Figure 2(a) shows the cartesian points generated by a mMIMO BS from 1000 UE locations in an urban scenario. The multi-path components for all sampled UE locations have clustered structures. If two sampled UE locations are close, then they have multi-path components in the same clusters. The clusters of LoS, single-bounce and double-bounce points have different densities; the cluster of LoS points is the densest, while a cluster of double-bounce points is sparser than single-bounce and LoS clusters. To construct a dissimilarity measure, we transform the features $\{f^{B}_{n}\}_{n=1}^{N}$ into cartesian points to guarantee that the cartesian points lie in a confined area, as shown in Figure 2(b). Then, we use density-based spatial clustering of applications with noise (DBSCAN) [10] to label these cartesian points. Figure 2(b) shows the clustering result for the above 1000 sampled UE locations.

Assuming that the multi-path components for all $N$ sampled UE locations are clustered into $C$ clusters and a component $x$ has a label $l(x) \in \{1, \ldots, C\}$, the dissimilarity metric for two samples $n$ and $m$ as in (8) is defined as

$$d_{J}(f^{B}_{n}, f^{B}_{m}) = \begin{cases} ||x_i - y_j||_2, & \text{if } n, m \text{ share the same clusters,} \\ ||x_i - y_j||_2, & \text{otherwise}, \end{cases} \quad (9)$$

where $[i, j] = \arg \max_{j} \{\min(\lambda_i, \mu_j)\}$ satisfying $l(x_i) = l(y_j)$. The core idea behind (9) is that if two samples share
We consider an urban outdoor multi-cell mmWave network scenario as depicted in Figure 3. The BSs are below rooftop, and signals will be reflected or blocked by walls. A ray-tracing channel model is used to generate the multi-path channels [14]. Table I summarizes the simulation parameters. We generate $N=5000$ UE locations on the streets of a Manhattan grid, as depicted in Figure 3, and gather estimated CSI samples from them. For SM and t-SNE, gradient descent is used to compute the channel charts, with initializations $Z_0$ drawn from the standard normal distribution. The number of nearest neighbors in LE and the perplexity for t-SNE are chosen to be $N/20$.

Figure 4 shows the multi-point channel charting results using SM, LE, and t-SNE based on the merged dissimilarities from multiple BSs. Performance of these three algorithms with different sets of participating BSs are investigated. The first row, Figures 4(a), 4(b), and 4(c) shows the results of SM, LE and t-SNE based on merged dissimilarities from four BSs $\{1, 3, 5, 7\}$. The second row shows results with six BSs $\{1, 3, 5, 7, 9, 10\}$, while the third row shows results with all 10 BSs. The channel charting performance improves when increasing the number of BSs, for all three algorithms, as more useful information is provided in the merged dissimilarity matrix. All three algorithms provide well-preserved local embeddings. With t-SNE, the global structure is well captured even with four BSs, as shown in Figure 4(c). It is remarkable that multipoint channel charting is able to perfectly capture the topology of the simulated Manhattan scenario, with ribbon-like streets and holes.

V. CONCLUSION

We have proposed multipoint channel charting, where CSI from multiple massive MIMO BSs is fused to provide a chart of the radio geometry of a multi-cell network. In contrast to single-point channel charting as proposed in [2], multiple BSs in the network measure the CSI from individual users, and construct CSI features from these measurements. The CSI features are fused in a central unit, and manifold learning techniques are applied to identify how the 2D (or 3D) spatial geometry of the user locations is embedded in the high-dimensional CSI space. We have developed improved CSI features based on direct estimation of incoming multi-path components, and created a novel dissimilarity measure based on clustering the information related to the estimated DoA and power of all separable multi-path components of set of sample users. We have demonstrated that multi-point channel charting, acting only on received CSI from sample users, can recover the street-topology of the network almost perfectly, significantly outperforming single-point channel charting.

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<tr>
<th>Table I</th>
<th>Simulation parameters of the considered system scenario.</th>
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<tr>
<td>Parameter</td>
<td>Symbol</td>
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<tr>
<td>Carrier frequency</td>
<td>$f_c$</td>
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<tr>
<td>System bandwidth</td>
<td>$b_{bw}$</td>
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<tr>
<td>OFDM subcarrier number</td>
<td>$N_c$</td>
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<tr>
<td>UE Tx power</td>
<td>$N_c \times P_{TXe}$</td>
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<td>BS noise power</td>
<td>$N_c \times \sigma^2$</td>
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Fig. 4. Multipoint charting results via SM, LE and t-SNE based on channel features from (a) BSs 1, 3, 5, 7; (b) BSs 1, 3, 5, 7, 9, 10; and (c) all 10 BSs. The multipoint charting performance improves with more participating BSs.

REFERENCES


